

講義中の注意



- 講義中は、参加者のマイク・カメラの機能はミュート状態になります。
- 進行はスタッフ及び講師が行いますので、指示に従ってください。
- 質疑応答の時間は、参加者のマイクをオンにして質問を受け付けることもあります。希望される方は「チャット欄」で申し出てください。

電験三種 ライブ講義

第7回 二次方程式

二次方程式

未知数の次数 (x^2) を含む方程式のことを二次方程式という

$$ax^2 + bx + c = 0 \quad (a \neq 0, b, c \text{は定数})$$

3パターンの計算手順

① $x^2 = A^2$ となる方程式

$$x^2 = 4 \rightarrow x^2 = 2^2 \rightarrow x = \pm 2$$

$$x^2 = 8 \rightarrow x^2 = (\sqrt{8})^2 \rightarrow x = \pm 2\sqrt{2}$$

② 因数分解を使った解法

$$x^2 + 3x + 2 = 0 \rightarrow (x + 2)(x + 1) = 0 \rightarrow x = -2, -1$$

$$x^2 - 4x + 4 = 0 \rightarrow (x - 2)^2 = 0 \rightarrow x = 2$$

③ 解の公式を使った解法

$$ax^2 + bx + c = 0 \rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

練習問題 I

(1) $x^2 = 9$

(2) $x^2 = 36$

(3) $x^2 = 144$

(4) $x^2 = 225$

Ans. $x =$

Ans. $x =$

Ans. $x =$

Ans. $x =$

(5) $x^2 = 8$

(6) $x^2 = 27$

(7) $x^2 = 40$

(8) $x^2 = 63$

Ans. $x =$

Ans. $x =$

Ans. $x =$

Ans. $x =$

練習問題 I

(1) $x^2 = 9$

(2) $x^2 = 36$

(3) $x^2 = 144$

(4) $x^2 = 225$

Ans. $x = \pm 3$

Ans. $x = \pm 6$

Ans. $x = \pm 12$

Ans. $x = \pm 15$

(5) $x^2 = 8$

(6) $x^2 = 27$

(7) $x^2 = 40$

(8) $x^2 = 63$

Ans. $x = \pm 2\sqrt{2}$

Ans. $x = \pm 3\sqrt{3}$

Ans. $x = \pm 2\sqrt{10}$

Ans. $x = \pm 3\sqrt{7}$

練習問題2

(1) $3x^2 - 2 = 10$

(2) $5x^2 - 30 = 15$

(3) $2x^2 + 2 = 100$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

(4) $2x^2 + 6 = 70$

(5) $3x^2 + 9 = 90$

(6) $5x^2 + 80 = 200$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

練習問題2

(1) $3x^2 - 2 = 10$

$$\begin{aligned} 3x^2 &= 12 \\ x^2 &= 4 \\ x &= \pm 2 \end{aligned}$$

Ans. $x = \pm 2$

(2) $5x^2 - 30 = 15$

$$\begin{aligned} 5x^2 &= 45 \\ x^2 &= 9 \\ x &= \pm 3 \end{aligned}$$

Ans. $x = \pm 3$

(3) $2x^2 + 2 = 100$

$$\begin{aligned} 2x^2 &= 98 \\ x^2 &= 49 \\ x &= \pm 7 \end{aligned}$$

Ans. $x = \pm 7$

(4) $2x^2 + 6 = 70$

$$\begin{aligned} 2x^2 &= 64 \\ x^2 &= 32 \\ x &= \pm\sqrt{32} = \pm 4\sqrt{2} \end{aligned}$$

Ans. $x = \pm 4\sqrt{2}$

(5) $3x^2 + 9 = 90$

$$\begin{aligned} 3x^2 &= 81 \\ x^2 &= 27 \\ x &= \pm\sqrt{27} = \pm 3\sqrt{3} \end{aligned}$$

Ans. $x = \pm 3\sqrt{3}$

(6) $5x^2 + 80 = 200$

$$\begin{aligned} 5x^2 &= 120 \\ x^2 &= 24 \\ x &= \pm\sqrt{24} = \pm 2\sqrt{6} \end{aligned}$$

Ans. $x = \pm 2\sqrt{6}$

因数分解を使った解法

② 因数分解を使った解法

$$x^2 + 3x + 2 = 0 \rightarrow (x + 2)(x + 1) = 0 \rightarrow x = -2, -1$$

$$x^2 - 4x + 4 = 0 \rightarrow (x - 2)^2 = 0 \rightarrow x = 2$$

因数分解

$$x^2 + (a + b)x + ab = (x + a)(x + b)$$

$$x^2 + 2ax + a^2 = (x + a)^2$$

$$x^2 - a^2 = (x + a)(x - a)$$

$$acx^2 + (ad + bc)x + bd = (ax + b)(cx + d)$$

因数分解を使った解法

$x^2 + (a + b)x + ab = (x + a)(x + b)$ の使い方

$$x^2 + \textcircled{5}x + \textcircled{6}$$

足して5、かけて6になる2つの数字を考える

$$= x^2 + (2 + 3)x + 2 \times 3$$

$$= (x + 2)(x + 3)$$

$$x^2 - \textcircled{1}x - \textcircled{6}$$

足して-1、かけて-6になる2つの数字を考える
→ 2つのうち1つの数は負の値

$$= x^2 + (2 - 3)x + 2 \times (-3)$$

$$= (x + 2)(x - 3)$$

因数分解を使った解法

$$x^2 + 2ax + a^2 = (x + a)^2 \text{の使い方}$$

$$x^2 + \textcircled{6}x + \textcircled{9}$$

2倍して6、2乗して9になる条件を満たす数字があれば

$$= x^2 + 2 \times 3x + 3^2$$

$$= (x + 3)^2$$

$$x^2 - \textcircled{14}x + \textcircled{49}$$

2倍して-14、2乗して49になる条件を満たす数字があれば

$$= x^2 + 2 \times (-7)x + (-7)^2$$

$$= (x - 7)^2$$

練習問題3

(1) $x^2 + x - 6 = 0$

(2) $x^2 - 3x + 2 = 0$

(3) $x^2 - 13x + 42 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

(4) $x^2 - 2x - 15 = 0$

(5) $x^2 - 8x - 48 = 0$

(6) $x^2 + 3x - 108 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

練習問題3

(1) $x^2 + x - 6 = 0$

$$(x + 3)(x - 2) = 0$$
$$x = -3, 2$$

Ans. $x = -3, 2$

(2) $x^2 - 3x + 2 = 0$

$$(x - 2)(x - 1) = 0$$
$$x = 2, 1$$

Ans. $x = 2, 1$

(3) $x^2 - 13x + 42 = 0$

$$(x - 7)(x - 6) = 0$$
$$x = 7, 6$$

Ans. $x = 7, 6$

(4) $x^2 - 2x - 15 = 0$

$$(x + 3)(x - 5) = 0$$
$$x = -3, 5$$

Ans. $x = -3, 5$

(5) $x^2 - 8x - 48 = 0$

$$(x + 4)(x - 12) = 0$$
$$x = -4, 12$$

Ans. $x = -4, 12$

(6) $x^2 + 3x - 108 = 0$

$$(x + 12)(x - 9) = 0$$
$$x = -12, 9$$

Ans. $x = -12, 9$

練習問題4

(1) $4x^2 + 11x + 6 = 0$

(2) $6x^2 - 19x + 10 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

(3) $12x^2 - x - 20 = 0$

(4) $8x^2 - 77x - 30 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

練習問題4

(1) $4x^2 + 11x + 6 = 0$

$\begin{array}{ccc} 1 & \rightarrow & 2 \\ 4 & \rightarrow & 3 \end{array}$ $\rightarrow 8$
 $\rightarrow 3$

$(x + 2)(4x + 3) = 0$
 $x = -\frac{1}{2}, -\frac{3}{4}$

Ans. $x = -\frac{1}{2}, -\frac{3}{4}$

(2) $6x^2 - 19x + 10 = 0$

$\begin{array}{ccc} 3 & \rightarrow & -2 \\ 2 & \rightarrow & -5 \end{array}$ $\rightarrow -4$
 $\rightarrow -15$

$(3x - 2)(2x - 5) = 0$
 $x = \frac{2}{3}, \frac{5}{2}$

Ans. $x = \frac{2}{3}, \frac{5}{2}$

(3) $12x^2 - x - 20 = 0$

$\begin{array}{ccc} 4 & \rightarrow & 5 \\ 3 & \rightarrow & -4 \end{array}$ $\rightarrow 15$
 $\rightarrow -16$

$(4x + 5)(3x - 4) = 0$
 $x = -\frac{5}{4}, \frac{4}{3}$

Ans. $x = -\frac{5}{4}, \frac{4}{3}$

(4) $8x^2 - 77x - 30 = 0$

$\begin{array}{ccc} 8 & \rightarrow & 3 \\ 1 & \rightarrow & -10 \end{array}$ $\rightarrow 3$
 $\rightarrow -80$

$(8x + 3)(x - 10) = 0$
 $x = -\frac{3}{8}, 10$

Ans. $x = -\frac{3}{8}, 10$

練習問題5

(1) $(x + 7)(x + 4) = 10$

(2) $(x + 3)(x + 1) = -1$

(3) $(x + 9)(x + 6) = 4$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

(4) $(x - 1)(x - 7) = -8$

(5) $(x - 6)(x - 7) = 6$

(6) $(x - 6)(x - 8) = 3$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

練習問題5

(1) $(x + 7)(x + 4) = 10$

$$\begin{aligned}x^2 + 11x + 28 &= 10 \\x^2 + 11x + 18 &= 0 \\(x + 2)(x + 9) &= 0 \\x &= -2, -9\end{aligned}$$

Ans. $x = -2, -9$

(2) $(x + 3)(x + 1) = -1$

$$\begin{aligned}x^2 + 4x + 3 &= -1 \\x^2 + 4x + 4 &= 0 \\(x + 2)^2 &= 0 \\x &= -2\end{aligned}$$

Ans. $x = -2$

(3) $(x + 9)(x + 6) = 4$

$$\begin{aligned}x^2 + 15x + 54 &= 4 \\x^2 + 15x + 50 &= 0 \\(x + 10)(x + 5) &= 0 \\x &= -10, -5\end{aligned}$$

Ans. $x = -10, -5$

(4) $(x - 1)(x - 7) = -8$

$$\begin{aligned}x^2 - 8x + 7 &= -8 \\x^2 - 8x + 15 &= 0 \\(x - 3)(x - 5) &= 0 \\x &= 3, 5\end{aligned}$$

Ans. $x = 3, 5$

(5) $(x - 6)(x - 7) = 6$

$$\begin{aligned}x^2 - 13x + 42 &= 6 \\x^2 - 13x + 36 &= 0 \\(x - 4)(x - 9) &= 0 \\x &= 4, 9\end{aligned}$$

Ans. $x = 4, 9$

(6) $(x - 6)(x - 8) = 3$

$$\begin{aligned}x^2 - 14x + 48 &= 3 \\x^2 - 14x + 45 &= 0 \\(x - 5)(x - 9) &= 0 \\x &= 5, 9\end{aligned}$$

Ans. $x = 5, 9$

練習問題6

(1) $(x - 1)(x - 8) = -3x$

(2) $(x + 9)(x + 4) = -2x$

(3) $(x - 3)(x - 4) = x$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

(4) $(x + 4)(x - 6) = 3x$

(5) $(x + 3)(x - 6) = 4x$

(6) $(x + 5)(x - 9) = 8x$

Ans. $x =$ _____

Ans. $x =$ _____

Ans. $x =$ _____

練習問題6

(1) $(x - 1)(x - 8) = -3x$

$$\begin{aligned}x^2 - 9x + 8 &= -3x \\x^2 - 6x + 8 &= 0 \\(x - 2)(x - 4) &= 0 \\x &= 2, 4\end{aligned}$$

Ans. $x = 2, 4$

(2) $(x + 9)(x + 4) = -2x$

$$\begin{aligned}x^2 + 13x + 36 &= -2x \\x^2 + 15x + 36 &= 0 \\(x + 12)(x + 3) &= 0 \\x &= -12, -3\end{aligned}$$

Ans. $x = -12, -3$

(3) $(x - 3)(x - 4) = x$

$$\begin{aligned}x^2 - 7x + 12 &= x \\x^2 - 8x + 12 &= 0 \\(x - 2)(x - 6) &= 0 \\x &= 2, 6\end{aligned}$$

Ans. $x = 6, 2$

(4) $(x + 4)(x - 6) = 3x$

$$\begin{aligned}x^2 - 2x - 24 &= 3x \\x^2 - 5x - 24 &= 0 \\(x + 3)(x - 8) &= 0 \\x &= -3, 8\end{aligned}$$

Ans. $x = -3, 8$

(5) $(x + 3)(x - 6) = 4x$

$$\begin{aligned}x^2 - 3x - 18 &= 4x \\x^2 - 7x - 18 &= 0 \\(x + 2)(x - 9) &= 0 \\x &= -2, 9\end{aligned}$$

Ans. $x = -2, 9$

(6) $(x + 5)(x - 9) = 8x$

$$\begin{aligned}x^2 - 4x - 45 &= 8x \\x^2 - 12x - 45 &= 0 \\(x + 3)(x - 15) &= 0 \\x &= -3, 15\end{aligned}$$

Ans. $x = -3, 15$

解の公式を使った解法

③解の公式を使った解法

$$ax^2 + bx + c = 0 \rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x^2 + x - 3 = 0$$

$a = 1, b = 1, c = -3$ を解の公式に代入する

$$\begin{aligned} x &= \frac{-1 \pm \sqrt{1^2 - 4 \times 1 \times (-3)}}{2 \times 1} = \frac{-1 \pm \sqrt{1 + 12}}{2} \\ &= \frac{-1 \pm \sqrt{13}}{2} \end{aligned}$$

練習問題7

(1) $x^2 + 3x + 1 = 0$

(2) $x^2 + 5x + 3 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

(3) $2x^2 - 3x - 3 = 0$

(4) $2x^2 + 3x - 4 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

練習問題7

(1) $x^2 + 3x + 1 = 0$

$$x = \frac{-3 \pm \sqrt{3^2 - 4}}{2}$$
$$x = \frac{-3 \pm \sqrt{5}}{2}$$

Ans. $x = \frac{-3 \pm \sqrt{5}}{2}$

(2) $x^2 + 5x + 3 = 0$

$$x = \frac{-5 \pm \sqrt{5^2 - 4 \times 3}}{2}$$
$$x = \frac{-5 \pm \sqrt{25 - 12}}{2}$$
$$x = \frac{-5 \pm \sqrt{13}}{2}$$

Ans. $x = \frac{-5 \pm \sqrt{13}}{2}$

(3) $2x^2 - 3x - 3 = 0$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \times 2 \times (-3)}}{2 \times 2}$$
$$x = \frac{3 \pm \sqrt{9 + 24}}{4}$$
$$x = \frac{3 \pm \sqrt{33}}{4}$$

Ans. $x = \frac{3 \pm \sqrt{33}}{4}$

(4) $2x^2 + 3x - 4 = 0$

$$x = \frac{-3 \pm \sqrt{3^2 - 4 \times 2 \times (-4)}}{2 \times 2}$$
$$x = \frac{-3 \pm \sqrt{9 + 32}}{4}$$
$$x = \frac{-3 \pm \sqrt{41}}{4}$$

Ans. $x = \frac{-3 \pm \sqrt{41}}{4}$

練習問題8

(1) $x^2 + 2x - 1 = 0$

(2) $2x^2 + 4x - 5 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

(3) $4x^2 + 6x + 1 = 0$

(4) $3x^2 + 8x - 5 = 0$

Ans. $x =$ _____

Ans. $x =$ _____

練習問題8

(1) $x^2 + 2x - 1 = 0$

$$x = \frac{-1 \pm \sqrt{1^2 - (-1)}}{1}$$
$$x = -1 \pm \sqrt{2}$$

Ans. $x = -1 \pm \sqrt{2}$

(2) $2x^2 + 4x - 5 = 0$

$$x = \frac{-2 \pm \sqrt{2^2 - 2 \times (-5)}}{2}$$
$$x = \frac{-2 \pm \sqrt{4 + 10}}{2}$$
$$x = \frac{-2 \pm \sqrt{14}}{2}$$

Ans. $x = \frac{-2 \pm \sqrt{14}}{2}$

解の公式を使った解法

$$ax^2 + 2bx + c = 0$$

$$\rightarrow x = \frac{-b \pm \sqrt{b^2 - ac}}{a}$$

(3) $4x^2 + 6x + 1 = 0$

$$x = \frac{-3 \pm \sqrt{3^2 - 4 \times 1}}{4}$$
$$x = \frac{-3 \pm \sqrt{9 - 4}}{4}$$
$$x = \frac{-3 \pm \sqrt{5}}{4}$$

Ans. $x = \frac{-3 \pm \sqrt{5}}{4}$

(4) $3x^2 + 8x - 5 = 0$

$$x = \frac{-4 \pm \sqrt{4^2 - 3 \times (-5)}}{3}$$
$$x = \frac{-4 \pm \sqrt{16 + 15}}{3}$$
$$x = \frac{-4 \pm \sqrt{31}}{3}$$

Ans. $x = \frac{-4 \pm \sqrt{31}}{3}$

ご聴講ありがとうございました!!